

# SCHOOLING-BY-SIZE IN THE BARENTS SEA CAPELIN STOCK 

by

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#### Abstract

This paper analyses the biological samples of capelin taken by the Institute of Marine Research, Bergen, on annual stock assesment surveys in the Barents Sea from 1972 to 1989. The dependency between mean length of 2 -year-olds and the mean age in the rest of the sample is demonstrated with the use of linear regression. The data from 1974 and 1978 are further analysed using a stepwise linear regression. The variation in mean length is best explained using the mean length of the capelin the 2 -year-olds are schooling with.


## INTRODUCTION

Like most other pelagic fish species, the capelin (Mallotus villosus) is sometimes
found to form schools. This is particularly significant during migration, e.g. when the mature capelin move towards the coasts to spawn. To a lesser degree, schooling also takes place during non migratory phases of
the capelins life cycle. In the Barents Sea, this is observed during September, when the capelin form feeding concentrations in the central and northern parts of the ocean, and the horizontal movements are limited. During this feeding season, the capelin is observed to form discrete schools at intermediate depths during daytime, and to disperse into loosely defined schools or layers during nighttime. At this time, a survey to assess the stock size and its geographical distribution is carried out annually by IMR in Bergen and PINRO in Murmansk. Acoustic methods are used, where both integration of echo signals and trawl sampling are used to calculate the stock size distributed on age and length groups. When analysing the biological data from a number of these surveys, it was found that there seemed to be a dependency between the mean length in each age group and the mean age in each sample, indicating the precence of a phenomenon called "schooling-by-size". This was most noticable with the two-year-olds, where the smallest individuals seemed to school together with the one-year-olds, while the largest individuals were found together with the three years old and older fish. Because of the possible consequences of division of the stock size estimate on age groups, and of an optimal sampling strategy, we decided to analyse this phenomenon more carefully. In this paper we analyse the precence of a dependency between age distribution and size distribution within samples, and try to explain such dependencies by linear regression models.

## MATERIALS AND METHODS

The basic data consists of various parameters measured on individual specimens of capelin in trawl samples, including age and length, together with data on the sample itself, viz. geographical position, depth,
number of individuals etc. Before these data were used in the analysis, mean values for length within age groups and age and length within samples were calculated. Data from the years 1972 to 1989 were included. All data were sampled at joint Norwegian/USSR surveys to assess the stock size and the geographical distribution of the Barents Sea capelin. These multiship surveys are carried out in September-October each year, and the resulting stock size estimates form the basis for the management advices concerning this stock given by ICES. The 1974 and 1978 data were choosen for a more detailed analysis, because the samples were particularly abundant these years, and a different dependency (slope) between the mean length of 2 -year-olds and the mean age in the rest of the sample was demonstrated.

When analysing the dependency between the mean length of the 2 -year group and the mean age (excluding 2 -year-olds) in a sample, we used an ordinary least square regression. Noting the mean length as $L_{2}$ and the mean age as $\mathrm{A}_{\mathrm{o}}$ we assume that the regression line is on the form :

$$
L_{2}=\beta_{0}+\beta_{1} A_{o}+\varepsilon
$$

The F-ratio were calculated as :

$$
F=\frac{M S_{\text {reg }}}{s^{2}}
$$

F follows a F -distribution under the nullhypothesis that $\beta_{1}=0$ and that the errors $\epsilon$ are independent and normally distributed $\mathrm{N}\left(0, \sigma^{2}\right)$.

The analysis of the 1974 and the 1978 data was done using a stepwise linear regression. In this way we could identify the most interesting variables for further analysis. For both years we used $\mathrm{L}_{2}$, the mean length of the 2 -year-olds as the dependent variable. The independent variables were $\mathrm{L}_{\mathrm{o}}$, the mean length in the sample excluding 2 -year-olds, $\mathrm{A}_{0}$, the mean age in the sample
excluding 2-year-olds, $\mathrm{N}_{1}$, the number of 1 -year-olds, $\mathrm{N}_{3}$, the number of 3 -year-olds, $\mathrm{N}_{4}$, the number of 4-year-olds and $\mathrm{N}_{3}+\mathrm{N}_{4}$, the number of both 3 and 4 -year-olds. All observations were weighted with the square root of $\mathrm{N}_{2} . \mathrm{N}_{2}$ is the number of 2-year-olds in the sample.

## RESULTS

Initially we wanted to investigate if there was any dependency between the mean length of 2 -year-olds and the mean age of capelin they were schooling with. The result for our initial regression analyses is shown in table 1. The table contains the estimated intercept ( $\beta_{0}$ ) and slope ( $\beta_{1}$ ). The table also include the test observator $F$ with its degrees of freedom and probability value. The degrees of freedom is $1, \mathrm{n}-2$ were n is the number of samples (observations) that year. As one can see there is significant dependencies (at the $5 \%$ level) between $\mathrm{L}_{2}$ and $\mathrm{A}_{\mathrm{o}}$ all years except 1988 and 1989. (Note the relative low number of samples in 1989). The percentage of variation explained (multiple $\mathrm{R}^{2}$ ) varies from 1.56 (1988) to 63.54 (1975).

Our 1974 data consists of 63 observations and our 1978 data of 59 observations. This is after 2 of the 1974 observations and 1 of the 1978 observations were deleted because of missing data. Weighted mean, estimated standard deviation (STD) and coefficient of variation (CV) is given in tables 2 and 3. The weighted correlation matrix is given in tables 4 and 5. Detailed results from each step in the regression analysis is given in tables 6 and 7. A relatively high degree of fit is demonstrated from the fact that the percentage of variation explained (multiple $\mathrm{R}^{2}$ ) is as high as $66.56 \%$ in the 1974 regression and $71.15 \%$ in 1978. The higher degree of fit in 1978 is in accordance with
the fact that the F-to-enter (or F-to remove) is higher. This can also be expected from the correlation matrix with a higher correlation between the dependent and the independent variables in 1978.

## DISCUSSION

One can see from table 1 that the slope is varying from 0.2103 (1988) to 1.6659 (1972). Very much of this variation can be explained from changes in the age composition. A very strong 2 -year old year class will dominate the material and little of the variation may be explained from "who" they are schooling with. Similarly will a relative high abundance of both 1 -year and 3 -year-olds give the 2 -year-olds larger possibilities to "choose" who to school with. Small (short) 2-year-olds tends to school with 1 -year-olds while large (long) 2 -year old "choose" to school with older capelin.

The more detailed regression analysis of the 1974 and the 1978 data shows us that the mean length of the capelin the 2 -year-olds are schooling with, gives a better fit than the mean age. This indicates that capelin form schools with individuals of approximately the same length. The mechanism behind this selection, is probably the need for approximately equal swimming speed among the individuals in a school, and swimming speed is coupled to body length. In addition to the mean length of capelin not in the 2 -yearolds group the number of 1 -year-olds and 3 -year-olds gave additional explanation of the variation in 1974 and 1978 respectively. The explanatory effect was significant, but not very large compared to the mean length.

These findings have obvious effects on survey strategies and on the use of agelength keys. The method used up to now for obtaining a stock size estimate partitioned on age groups, is based on the assumptions
that the length and age distribution obtained by sampling within a subarea are representative for that subarea. The results reffered to in this paper may question both.

Firstly, the total length distribution may be biased by chance alone when the number of samples within a subarea becomes very small. This will lead to errors in the total stock size estimate in numbers, since the conversion factor between echo-values and number of fish is length-dependent for capelin.

Secondly, the partition of the total number of fish on age groups may also be wrong,
again if the number of samples become small.

However, if the number of samples are large, and if the probability of sampling a school of one particular length-age composition reflects a true proportion of a population, then the problem caused by schooling-by-size may be negligible.

Further work will be undertaken to investigate if some kind of correcting agelength keys based on conditional age or length distributions can diminish this problem even when a small number of samples are taken within one subarea.

TABLE 1.

| Year | Intercept | Slope | F | d.f. | P (Tail) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1972 | 8.10922 | 1.6659 | 10.493 | 1,11 | 0.0079 |
| 1973 | 10.13791 | 0.9919 | 25.559 | 1,30 | 0.0000 |
| 1974 | 11.13375 | 0.3441 | 5.500 | 1,63 | 0.0222 |
| 1975 | 9.54897 | 1.0689 | 43.569 | 1,25 | 0.0000 |
| 1976 | 11.59829 | 0.4609 | 16.663 | 1,49 | 0.0002 |
| 1977 | 10.25114 | 0.8975 | 85.693 | 1,57 | 0.0000 |
| 1978 | 9.89622 | 0.8761 | 64.699 | 1,58 | 0.0000 |
| 1979 | 10.57554 | 0.7165 | 66.589 | 1,51 | 0.0000 |
| 1980 | 11.66978 | 0.6708 | 58.866 | 1,68 | 0.0000 |
| 1981 | 11.72500 | 0.5275 | 13.056 | 1,63 | 0.0006 |
| 1982 | 11.23060 | 0.7615 | 43.917 | 1,59 | 0.0000 |
| 1983 | 10.54208 | 1.3012 | 60.517 | 1,75 | 0.0000 |
| 1984 | 10.44154 | 1.0943 | 31.399 | 1,64 | 0.0000 |
| 1985 | 11.45771 | 0.5704 | 20.740 | 1,64 | 0.0000 |
| 1986 | 10.22968 | 1.4297 | 33.782 | 1,31 | 0.0000 |
| 1987 | 11.57195 | 1.0394 | 6.710 | 1,14 | 0.0214 |
| 1988 | 13.49643 | 0.2103 | 0.587 | 1,37 | 0.4483 |
| 1989 | 12.93821 | 0.8259 | 2.853 | 1,16 | 0.1106 |

TABLE 2. (1974)
TABLE 3.
(1978)

| Variable <br> name | Weighted <br> mean | STD | CV |  | Variable <br> name | Weighted <br> mean | STD | CV |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L2 | 11.9138 | 1.7678 | 0.148382 |  | L2 | 11.8884 | 2.6135 | 0.219832 |
| Lo | 12.2750 | 3.5245 | 0.287124 |  | Lo | 12.8117 | 5.2714 | 0.411450 |
| Ao | 2.3403 | 1.4382 | 0.614531 |  | Ao | 2.3138 | 2.1087 | 0.911358 |
| N1 | 9.6436 | 27.1187 | 2.812086 |  | N1 | 6.4747 | 29.2522 | 4.517892 |
| N3 | 16.7536 | 26.9448 | 1.608300 |  | N3 | 7.5557 | 23.8279 | 3.153643 |
| N4 | 0.7125 | 4.3727 | 6.137393 |  | N4 | 0.7756 | 3.5241 | 4.543744 |
| N3+N4 | 17.4660 | 29.4377 | 1.685427 |  | N3+N4 | 8.3313 | 26.7253 | 3.207836 |

TABLE 4.
(1974)

|  | L2 | Lo | Ao | N1 | N 3 | N 4 | $\mathrm{~N} 3+\mathrm{N} 4$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L2 | 1.0000 |  |  |  |  |  |  |
| Lo | 0.6573 | 1.0000 |  |  |  |  |  |
| Ao | 0.2631 | 0.7957 | 1.0000 |  |  |  |  |
| N1 | 0.0246 | -0.5677 | -0.8475 | 1.0000 |  |  |  |
| N3 | 0.4788 | 0.8065 | 0.6980 | -0.4375 | 1.0000 |  |  |
| N4 | 0.4684 | 0.6494 | 0.3694 | -0.1943 | 0.5154 | 1.0000 |  |
| $\mathrm{~N} 3+\mathrm{N} 4$ | 0.5079 | 0.8347 | 0.6938 | -0.4293 | 0.9919 | 0.6203 | 1.0000 |

TABLE 5.
(1978)

|  | L2 | Lo | Ao | N1 | N 3 | N 4 | $\mathrm{~N} 3+\mathrm{N} 4$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L2 | 1.0000 |  |  |  |  |  |  |
| Lo | 0.7880 | 1.0000 |  |  |  |  |  |
| Ao | 0.7304 | 0.9426 | 1.0000 |  |  |  |  |
| N1 | -0.5379 | -0.6839 | -0.6661 | 1.0000 |  |  |  |
| N3 | 0.7442 | 0.6562 | 0.5346 | -0.3026 | 1.0000 |  |  |
| N4 | 0.6010 | 0.5677 | 0.4537 | -0.2552 | 0.7982 | 1.0000 |  |
| $\mathrm{~N} 3+\mathrm{N} 4$ | 0.7427 | 0.6599 | 0.5364 | -0.3034 | 0.9968 | 0.8435 | 1.0000 |

TABLE 6. (1974)

| STEP NO. 0 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| ANOVA : | SS | df | MS |  |
| Residual | 193.75668 | 62 | 3.125108 |  |
| Variable | Coefficient | F-to-remove | Variable (not in eq.) | F-to-enter |
| Intercept | 11.91383 |  |  |  |
|  |  |  | Lo | 46.41 |
|  |  |  | Ao | 4.54 |
|  |  |  | N1 | 0.04 |
|  |  |  | N3 | 18.15 |
|  |  |  | N4 | 17.14 |
|  |  |  | N3+N4 | 21.20 |
| STEP NO. 1 |  |  |  |  |
| ANOVA : | SS | df | MS | F Ratio |
| Regression | 83.714729 | 1 | 83.71473 | 46.41 |
| Residual | 110.04195 | 61 | 1.803966 |  |
| Variable | Coefficient | F-to-remove | Variable (not in eq.) | F-to-enter |
| Intercept | 7.86681 |  |  |  |
| Lo | 0.32969 | 46.41 | Ao | 28.79 |
|  |  |  | N1 | 41.89 |
|  |  |  | N3 | 0.81 |
|  |  |  | N4 | 0.32 |
|  |  |  | N3+N4 | 0.59 |
| STEP NO. 2 |  |  |  |  |
| ANOVA : | SS | df | MS | F Ratio |
| Regression | 128.95567 | 2 | 64.47784 | 59.70 |
| Residual | 64.801003 | 60 | 1.080017 |  |
| Variable | Coefficient | F-to-remove | Variable (not in eq.) | F-to-enter |
| Intercept | 5.44610 |  |  |  |
| Lo | 0.49684 | 119.29 | Ao | 1.01 |
| N1 | 0.03826 | 41.89 | N3 | 2.09 |
|  |  |  | N4 | 1.25 |
|  |  |  | N3+N4 | 2.75 |

TABLE 7. (1978)

| STEP NO. 0 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| ANOVA : | SS | df | MS |  |
| Residual | 396.15189 | 58 | 6.830205 |  |
| Variable | Coefficient | F-to-remove | Variable (not in eq.) | F-to-enter |
| Intercept | 11.88844 |  |  |  |
|  |  |  | Lo | 93.35 |
|  |  |  | Ao | 65.18 |
|  |  |  | N1 | 23.20 |
|  |  |  | N3 | 70.74 |
|  |  |  | N4 | 32.24 |
|  |  |  | N3+N4 | 70.14 |
| STEP NO. 1 |  |  |  |  |
| ANOVA : | SS | df | MS | F Ratio |
| Regression | 245.96025 | 1 | 245.9603 | 93.35 |
| Residual | 150.19164 | 57 | 2.634941 |  |
| Variable | Coefficient | F-to-remove | Variable (not in eq.) | F-to-enter |
| Intercept | 6.88347 |  |  |  |
| Lo | 0.39066 | 93.35 | Ao | 0.20 |
|  |  |  | N1 | 0.00 |
|  |  |  | N3 | 17.58 |
|  |  |  | N4 | 5.67 |
|  |  |  | N3+N4 | 16.91 |
| STEP NO. 2 |  |  |  |  |
| ANOVA : | SS | df | MS | F Ratio |
| Regression | 281.84915 | 2 | 140.9246 | 69.04 |
| Residual | 114.30274 | 56 | 2.041120 |  |
| Variable | Coefficient | F-to-remove | Variable (not in eq.) | F-to-enter |
| Intercept | 8.21540 |  |  |  |
| Lo | 0.26089 | 30.60 | Ao | 0.87 |
| N3 | 0.04375 | 17.58 | N1 | 1.29 |
|  |  |  | N4 | 0.14 |
|  |  |  | N3+N4 | 0.14 |








1982
1983


1985



1989


